

RESEARCH OF NEURONAL MORPHOLOGY'S CLASSIFICATION AND RECOGNITION

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ABSTRACT

By comparing cluster analysis, BP neural network, This paper establishes a classification model based on fuzzy clustering identification, and has obtained good classification results; analyzes the same neurons' different characteristics in different animals, obtaining aggregates of neurons can better classify neurons, but can not distinguish the different morphological characteristics in different animals, The use of the component indicators of neurons can distinguish them clearly.

Keywords: *Classification of neurons; Cluster Analysis; Neural network; Fuzzy Clustering.*

1. INTRODUCTION

How to identify and distinguish different types' neurons accurately is of great significance to Human Brain Project (HBP), at present, the science still have not solved this issue. Vivisection distinguishing neurons is mainly through geometric shape and potential distribution these two factors. The use of neurons' potential distribution pattern is more complex, is mainly related to neuron' Hodgkin-Huxley model and the discrete form of rall cable model. This paper studies how to use geometric features of neurons, by mathematical modeling, gives a space shape's classification of neurons, and classifies neurons accurately.

1.1. Data source

Neuronmorpho.org [1] contains a large number of geometric shape data of neurons, Here, we select two sets of data, A set of data is the control group, has 43 different types' neurons(Grouped); B set of data is feature group, including Motor neurons, purk neurons, pyramidal neurons, intermediate neurons, sensory neurons, seven of five kind neurons which is Known of classification,(intermediate neurons can be divided into three categories: Bipolar, tripolar, multipolar Intermediate neurons).

In order to classify more precisely, using LM [2] to calculate 21 geometry value of the 50 neurons samples in A, B.

Table 1. Geometric characteristics of neurons usually used

No.	Geometric characteristics	The select of LM computing result	No.	Geometric characteristics	The select of LM computing result
1	Cell body area	Total_sum	12	Euclidean distance	max
2	The number of stems	Total_sum	13	Path distance	max
3	The number of bifurcations	Total_sum	14	Branch_Order	max
4	The number of branch	Total_sum	15	Contraction	avg
5	Width	avg	16	Fragmentation	Total_sum
6	Height	avg	17	Partition_asymmetry	avg
7	Depth	avg	18	Roll rate	avg
8	Diameter	avg	19	Local bifurcation angle	avg
9	Length	Total_sum	20	Far Bifurcation angle	avg
10	Surface	Total_sum	21	Fractal dimension	avg
11	Volume	Total_sum			

Notes: English name and Interpretation is consistent with it used in L-Measure software, The select of LM computing result refers to the document of LMeasure_contest_help.doc, Uncharted characteristic index computing results Choose the average value.

2. THE CLASSIFICATION OF NEURONS

Using Neurons geometric data in A and B, Find out the geometric characteristics of five kinds of neurons in B, give a methods of morphological classification of neurons.

2.1. Cluster Analysis

Known by the principal component analysis, the first four eigenvalue in 21 Characteristics indicators is greater than

1, together they explain 95.594% of the total variance, although the fifth explain 3.039% of the total variance, but its characteristic value is 0.649 and less than 1. This shows that the explanatory power of principal components is not more than the average explanatory power of directly introducing of the original variables. Therefore, only need to extract the first four principal components. Use these four principal components to replace the original 21 variables and to do clustering and classification identification.

Observing the initial factor loading matrix, we can know cell surface area, the number of the stems, width, height, depth, diameter, length, surface area, volume, Euclidean distance, path distance, Roll rate and Fractal dimension in the first principal component F_1 has a very high load, this indicates F_1 basically reflects geometric contour information of neurons space shape. Number of bifurcations、Branching number、Roll rate and fractal dimension in the second principal component F_2 has a very high load, this indicates F_2 basically reflects bifurcation and the branch information of neurons space shape. Contraction, proximal bifurcation angle and remote bifurcation angle in the third principal component F_3 has a very high load, this indicates F_3 basically reflects flexibility and scalability of neurons space shape. Asymmetric division in the fourth principal component F_4 has a very high load, this indicates F_4 basically reflects symmetry of neurons space shape.

The Variable coefficient vector of the i (“ i ” represent for first, second, third, fourth, fifth) principal components F_i is obtained by the i column vector of the initial factor loading matrix dividing the square root of the i characteristic root, That is :

$$\begin{aligned}
 F_1 &= 0.286538ZX_1 + 0.278449ZX_2 + \dots - 0.254683575ZX_{21} \\
 F_2 &= 0.029575ZX_1 + 0.002247ZX_2 + \dots - 0.09569ZX_{21} \\
 F_3 &= 0.059618ZX_1 + 0.039195ZX_2 + \dots + 0.256065ZX_{21} \\
 F_4 &= -0.09962ZX_1 + 0.216156ZX_2 + \dots + 0.093193ZX_{21}
 \end{aligned}$$

Substitute F_i into comprehensive evaluation function $F_z = \sum_{i=1}^m (\lambda_i / k) F_i$, here $k=21$, thus:

$$F_z = 0.558544F_1 + 0.202454F_2 + 0.125172F_3 + 0.069768F_4$$

Calculating the score of each principal component and also referencing to the control group data to divide the sample into five intervals, We obtained the correct rate of 90.4%. While dividing into seven intervals, the correct rate is 67.7% only, Misjudgment rate is high, we will try other methods.

2.2. BP Neural Network

BP neural network is one of the most widely used and the most successful network[3], can be a good solution to the complex causal relationship and non-deterministic reasoning, judging, identification and classification Problem.

Based on previous principal component analysis, We have 21 indicator variables down into four, Therefore, in the design of BP neural network [4] , the number of the input layer elements is 4, that is $N_{in}=4$; Since we have five classes of neurons, Therefore, the number of the output layer elements is 3, that is $N_{out}=3$, This can Characterize 8 kind of neurons, and includes unknown neurons In addition to 5 kinds. in order to ensure the accuracy and convergence rate of the Network training, We will set the network training error of 1×10^{-5} .

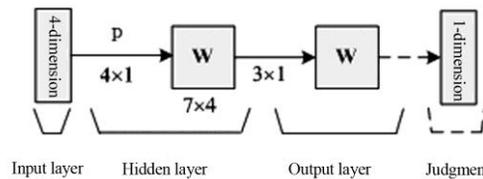


Fig. 1: Neural network computing flow chart

The calculation shows that, Using the 21 neural network indicators, the accuracy rate of Clustering Class 7 is 69.17% ; in the 21 neural network indicators, the accuracy rate of Clustering Class 5 is 95.45% ; Because the study sample is relatively few, only seven, so the deviation of the results is also evident.

2.3. Fuzzy Clustering

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Fuzzy Mathematics is an important tool for studying uncertain phenomena, for neuron classification problem, Fuzzy Mathematics [5] theory, can also be used to modeling and solving. The main point is to establish fuzzy similar matrix $R_{ij}=(r_{ij})_{51 \times 21}$, and then use transitive closure to do cluster analysis, and can draw dynamic clustering diagram. In the 21 indicators, the deviation of clustering recognition is also obvious, the accuracy rate is 33/51=65% under 70%, This shows that we only use 21 indicators data, the deviation of clustering recognition is inevitable. So we re-process the data, establish 43 effective indicators, After several trials of different data, we Obtain recognition method using fuzzy clustering, the deviation of recognition achieves minimum, results are as followings:
 Result one: when range transformation $\lambda=0.4619$, the correct rate of clustering 5 classes was 96.1%, but further divided into 7 classes, the correct rate is only 76.5%, shown as figure 2.

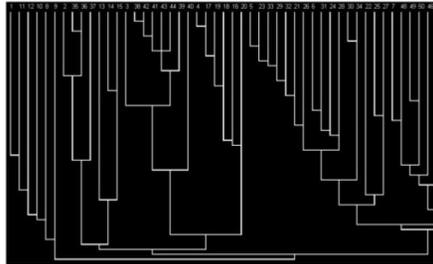


Fig. 2: Range transformation clustering diagram

Result two: the 45 set of data, Known as divided into motor neurons and purk neurons, When $\lambda=0.4349$, Classification accuracy rate is 99.2%, shown as figure 3.

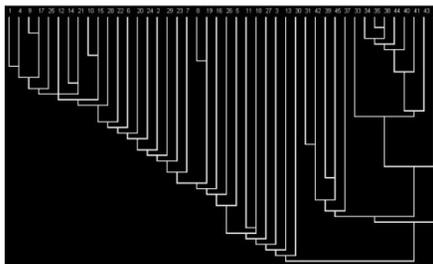


Fig. 3: Standard deviation transform clustering diagram

Thus, we verified, Fuzzy clustering recognition method, In neurons classification problems, Indeed has advantages ; Through the known types of neurons, distinguish similar types of neurons.

Calculation program is as follows:

step one: Data Standardization.

Apply shift standard deviation transformation and shift range transformation to standardize data.

Step two: Calibration(establish fuzzy similar matrix).

Apply exponent similarity coefficient method

$$r_{ij} = \frac{1}{m} \sum_{k=1}^i \exp \left[-\frac{3}{4} \frac{(x_{ki} - x_{jk})^2}{s_k^2} \right] \text{ And, } s_k = \frac{1}{n} \sum_{k=1}^i (x_{ik} - \bar{x}_{ik})^2$$

Establish fuzzy similar matrix $R_{ij}=(r_{ij})_{51 \times 21}$

Step three: Use the method of transitive closure to do cluster analysis.

Transitive closure is the clustering method based on the fuzzy equivalent matrix, For different $\lambda \in [0, 1]$, we can obtain different classification, and then get different dynamic clustering graph, Therefore, determining the threshold λ becomes the key factor for classification. Method of determining the threshold λ usually includes subjective judgments and the use of statistics F to determine the appropriate value λ .

$$F = \frac{\sum_{j=1}^r n_j \frac{\| \overline{x_k^{(j)}} - \overline{x} \|^2}{(r-1)}}{\sum_{i=1}^r \sum_{i=1}^{n_j} \frac{\| x_i^{(j)} - \overline{x_k^{(j)}} \|^2}{(n-r)}}$$

And

$$\overline{x_k^{(j)}} = \frac{1}{n_j} \sum_{i=1}^{n_j} x_{ik}^{(j)} \quad (k = 1, 2, \dots, m), \quad \overline{x_k} = \frac{1}{n} \sum_{i=1}^n x_{ik} \quad (k = 1, 2, \dots, m), \quad \overline{x} = (\overline{x_1}, \overline{x_2}, \dots, \overline{x_n})$$

Step four: Dynamic clustering of fuzzy cluster analysis.

Step five: Call the main program, input data, output dynamic clustering diagram.

The following is the clustering results of 43 indicators parameter dividing into 5 classes:

$\lambda=0.4556$

{ 1 11 12 10 8 9 } → □ Motor neurons

{ 2 35 36 37 13 14 15 } □ → purk neurons

{ 3 38 42 41 43 44 39 40 } → □ Pyramidal neurons

{ 4 17 19 18 16 20 } □ → Sensory neurons

{ 5 23 33 29 32 21 26 6 31 24 28 30 34 22 25 27 7 48 49 50 46 45 51 47 } □ → Intermediate neurons

This can be seen that only two classification results are not correct, Accuracy was 96%. However, if it is divided into 7 classes, 12 results is not correct, Accuracy dropped to 76.5%.

Use of F – distribution to examine the effectiveness of λ , when $n = 51, r = 5, f = 21.1228$; when

$n = 51, r = 7, f = 13.6861$; when $\alpha = 0.05$, Look-up table: $F_\alpha(4, 47) \leq 2.61, F_\alpha(7, 47) \leq 2.25$,

Obviously, it is valid for the classification.

In order to obtain each group’s classification geometric characteristics, We take the group number $t=[6,7,8,22,8]$,

t_i : represent the i group’s samples number, $x = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1m} \\ x_{21} & x_{22} & \dots & x_{2m} \\ \dots & \dots & \dots & \dots \\ x_{n1} & x_{n2} & \dots & x_{nm} \end{bmatrix}$ is the normalized data matrix, make:

$$\overline{x_k^{(i)}} = \frac{1}{t(i)} \sum_{i=0}^{t(i)} x_{ik} ; \quad \overline{x_k} = \frac{1}{n} \sum_{i=1}^n x_{ik} ; \quad , \text{make } f_1 = \sum_{j=1}^r \left| \overline{x_k^{(j)}} - \overline{x_k} \right|, \quad f_2 = \sum_{j=1}^r \sum_{i=0}^{t(i)} \left| x_{ik} - \overline{x_k^{(j)}} \right| ; \quad \text{then}$$

$$f = \frac{f_1(n-r)}{f_2(r-1)}$$

reflects the gap between each group and gap within each group. It is not difficult to prove: the

bigger f is, the more it can reflect indicators rates between each group, so, sort by the elements of f , Find the geometric characteristics whose current classification impact is the greatest and then could well reflect the spatial morphology of neurons.

$m=21$, that take 21 indicators, 6 geometric characteristics which are obvious in each group are:

Motor	Purk	Pyramidal	Sensory	Interneuron
N_stems	EucDistance	SectionArea	Euc Distance	N_stems
N_bifs	Volume	N_stems	N_stems	Terminal_degree
N_branch	N_branch	EucDistance	Volume	SectionArea
Surface	N_bifs	Branch_Order	TerminalSegment	SectionArea
SectionArea	SectionArea	N_tips	SectionArea	N_bifs
Terminal_degree	N_stems	Terminal_degree	N_branch	Length

m=43, that take 43 indicators, 11 geometric characteristics which are obvious in each group are:

Motor	Purk	Pyramidal	Sensory	Interneuron
Taper_1	Pa_Dr_Ratio	Taper_1	TerminalSegment	Taper_1
Fractal_Dim	TerminalSegment	Pa_Dr_Ratio	Fragmentation	N_branch
Pk_2	Fragmentation	Pk_classic	Taper_1	Type
Pk_classic	Taper_1	Pk_2	Daughter_Ratio	TerminalSegment
N_stems	Contraction	Pk	N_stems	N_stems
Diam_threshold	Daughter_Ratio	Branch_Order	Diam_threshold	Pa_Dr_Ratio
N_bifs	N_branch	N_stems	Pk	Diam_threshold
Pk	N_tips	Bif_ampl_remote	Pa_Dr_Ratio	Branch_Order
N_branch	Terminal_degree	Daughter_Ratio	Contraction	Daughter_Ratio
N_tips	N_bifs	Helix	Branch_Order	Pk_classic
Terminal_degree	Branch_Order	Fragmentation	Bif_ampl_local	PathDistance

3. CLASSIFICATION OF SIMILAR NEURONS IN DIFFERENT ANIMALS

The morphology of neurons is complex and diverse, different animals have different neurons, the same animals also have different neurons, Similar neurons in different animals also have differences. Then when distinguish morphological characteristics of same type of neurons in different animals, the parameters of distinguishing features should be selected to reflect the following three aspects:

- Such morphological features can well represent the characteristics of this class of neurons;
- At the same animals species, dissimilarity of such neurons' morphological characteristics should be as small as possible;
- At the different animals species, dissimilarity of such neurons' morphological characteristics should be as big as possible;

3.1. Model Based On Tree Structure

Due to the similarity of tree structure[6] and the morphology of neurons, using a tree structure model to simulate the geometry distribution of neurons is just right.

3.2. The Selection Of Morphological Features

Tree structure-based neuron model inherits all the advantages of tree model; it is benefit for the statistics of the details of the neurons' characteristics; get more detail information, contribute to distinguish of similar neurons in different animals' nervous system. When selected morphological parameters, the following two characteristics are for reference:

Characteristic one: Branch length

Neurons' tee structure, from the lowest level, where the nerve endings exist, as a starting point, travel turn to the root node which is labeled one, find out the length of each nerve endings to the AV which is labeled one, take all the length values as parameters of this kind of morphological characteristics.

In the three-dimensional space where Neurons located, the distance formula between two adjacent AV a_1 and a_2

$$\text{is: } d_1 = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2 + (z_1 - z_2)^2}$$

Among, the space coordinates of a_1 is (x_1, y_1, z_1) , the space coordinates of a_2 is (x_2, y_2, z_2) , then the branch length formula from one nerve ending to the AV which is labeled "one" is $l = d_1 + d_2 + d_3 + \dots + d_n$, Among, n is the number of branch from nerve ending to the AV which is labeled "one".

Characteristic two: Number of sub-AV

Number of sub-AV is defined as the number of AV which is non-home AV and associated with this AV. through traversing and searching the generated neurons tree to obtain the number of AV whose number of sub-AV is 0. Similarly, we can in turn obtain the number of AV whose number of sub-AV is 1,2,..... . So we can use the number of sub-AV as indicators of distinguishing morphological characteristics.

Table 2. Relationship table of home AV and sub-AV

AV label	Home AV label	Number of sub-AV	sub-AV label
B	A	2	C and D
C	B	2	E and F
E	C	1	G
F	C	1	H

We can know from the analysis of table 2, AV A, AV C and AV D are connected with AV B, among them, AV A and AV B are home AV, AV C and AV D are sub-AV of AV B. As shown in the table, the number of sub-AV of AV B is two, and the sub-AV is C and D respectively; the number of sub-AV of AV C is also two, and the sub-AV is E and F respectively; the number of sub-AV of AV E is one, and its sub-AV is G; the number of sub-AV of AV F is one, and its sub-AV is H; By traversing the entire neurons tree structure model we can obtain each AV's corresponding number of sub-AV, can use number of sub-AV as morphology Indicators of judgment. Following takes pig's purk neurons and mouse's purk neurons as examples, by tree model calculating obtain the following morphological characteristics value:

Table 3. Comparison of Purk neurons morphological characteristics of Mouse and Pig

	Mouse	Pig
The length of longest single nerve	390.882363	267.225337
The total number of AV whose branch number is 0	418	343
The total number of AV whose branch number is 1	547	1907
The total number of AV whose branch number is 2	417	342

Analysis shows: for purk neurons, in these extracted characteristics, there are two most prominent features, One is the length of the longest single nerve, neurons belong to the pig, its length of the longest single nerve is very close; Neurons belong to the mouse, is also very close, but pig's length of the longest single nerve is far less than mouse; the other is the total number of AV whose branch number is 1, the total number of AV who belongs to pig and whose branch is one, is very close, AV who belongs to mouse, is also very close, but the total number of AV who belongs to pig and whose branch number is one, is far more than mouse. We can see from the classification results that, by choosing above two morphological characteristics, we can well distinguish which animals this kind of neurons belong to.

4. CONCLUSIONS

This paper analyze the complexity of diversity of neurons space shape, through a variety of methods, trial again and again, Using cluster analysis, neural network algorithms, etc, finally, by comparison, establishes a classification method of fuzzy clustering. On known data, obtained better classification results, when $\lambda=0.4556$, classify neurons in A, B, The results is 96% correct, But further divided into 7 class, in this level the accuracy is only 76.5%.

Using online data, and the classification algorithm written and designed by myself, analyze similar neurons' different characteristics in different animals. We obtains that, aggregate indicators of neurons can better classify neurons, but can not distinguish the morphological characteristics of different animals, while using the component indicators of neurons can distinguish them clearly. For example, using single nerve branch' longest length and the total number of non-branching AV, can distinguish purk neurons between pig and mouse.

In addition, the author generates a new idea, puts forward the new concept of flat level (flat level: Neurons are known as a certain width, height and depth ,they are w, h, d, mark $\alpha=\min(w, h, d)$, The other two larger variables

are denoted as b, c, then neurons flat level can be defined as $\frac{a}{\sqrt{b^2 + c^2}}$), neurons flat level is a important

geometry which reflect neurons space shape, purk neurons projection difference in different coordinate plane, the shape of purk is similar to two-dimensional. If adding flat level into the process of classification of neurons, it should improve the classification accuracy in a certain extent, It remains need follow-up experiments.

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